photographs confirmed that the crystals are orthorhombic with,
$a=6.290 \pm 0.003, b=9.318 \pm 0.005, c=15.39 \pm 0.01 \AA$.
These give $0.674: 1: 1.652$ for the axial ratios. Taking the density to be $1.548 \mathrm{~g} . \mathrm{cm} .^{-3}$ (the mean of the two values, 1.542 and 1.553 g.cm. ${ }^{-3}$ given by Groth), the unit cell contains 4 molecules of $\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{7} . \mathrm{H}_{2} \mathrm{O}$ per unit cell (density calculated $=1.546 \mathrm{~g} . \mathrm{cm}^{-3}$ ).

The only systematic absences were $h 00$ absent when $h$ is odd, $0 k 0$ when $k$ is odd and $00 l$ when $l$ is odd. The space group is therefore $D_{2}^{4}-P 2_{1} 2_{1} 2_{1}$. This space group is not consistent with the crystal class quoted by Groth. Quite apart from the absent reflexions, the class $m m m$ is unlikely to be correct with a unit cell containing only 4 molecules as it would mean that each molecule of citric acid and the molecule of water would have to possess some element of symmetry.

## Potassium citrate monohydrate

Crystals of this substance are monoclinic, with

$$
\begin{gathered}
a=7 \cdot 06 \pm 0.03, \quad b=11 \cdot 72 \pm 0.05, \quad c=13.69 \pm 0.07 \AA ; \\
\beta=112 \cdot 0^{\circ} .
\end{gathered}
$$

The density determined by flotation is 2.00 g.cm. ${ }^{-3}$, giving 4 molecules of $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{O}_{7} \mathrm{~K}_{3} . \mathrm{H}_{2} \mathrm{O}$ per unit cell (density calculated $=2.050$ g.cm. ${ }^{-3}$ ). Systematic absences were $h 0 l$ when $l$ is odd and $0 k 0$ when $k$ is odd. The space group is therefore $C_{2 h}^{5}-P 2_{1} / c$.

## Sodium citrate dihydrate

Groth gives this substance as monoclinic prismatic (2/m), with $a: b: c=0.8923: 1: 1.3647, \beta=115^{\circ} 55^{\prime}$. X-ray photographs gave
$a=11.23 \pm 0.05, \quad b=12.501 \pm 0.002, c=15.82 \pm 0.08 \AA$; $c \sin \beta=15 \cdot 262 \pm 0 \cdot 003 \AA, \beta=104^{\circ} 22^{\prime}$.

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If the same $c$ axis is chosen as that of Groth we get $c^{\prime}=16.98 \AA$ and $\beta^{\prime}=115^{\circ} 49^{\prime}$, giving axial ratios of $a: b: c^{\prime}=0 \cdot 898: 1: 1 \cdot 358$. The density determined by flotation is $1.84 \mathrm{~g} . \mathrm{cm} .^{-3}$ and there are 8 molecules of $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{O}_{7} \mathrm{Na}_{3} .2 \mathrm{H}_{8} \mathrm{O}$ per unit cell (density calculated $=1.823 \mathrm{~g} . \mathrm{cm} .^{-3}$ ). Systematic absences were: $h k l$ when ( $k+l$ ) is odd, $h 0 l$ when $h$ or $l$ is odd and $0 k 0$ when $k$ is odd. There are two space groups available $C_{s}^{4}-A a$ and $C_{2 h}^{6}-A 2 / a$. If the classification given by Groth is correct then the latter space group is the appropriate one.

## Sodium citrate pentahydrate

This compound is given by Groth as rhombic bisphenoidal (222) with axial ratios $a: b: c=0.6208: 1: 0 \cdot 2431$. X-ray photographs confirmed that the crystals are orthorhombic with

$$
a=6.41 \pm 0.03, \quad b=16.36 \pm 0.08, \quad c=26.31 \pm 0.10 \AA
$$

These give axial ratios $b: c: a=0.6218: 1: 0.2436$. The density determined by flotation is $1.70 \mathrm{~g} . \mathrm{cm} .^{-3}$, which differs appreciably from the value given by Groth $\left(1.857-1.859 \mathrm{~g} . \mathrm{cm} .^{-3}\right)$. The calculated density, using the above unit-cell dimensions and assuming 8 molecules of $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{O}_{7} \mathrm{Na}_{3} .5 \mathrm{H}_{2} \mathrm{O}$ per unit cell, is $1.68 \mathrm{~g} . \mathrm{cm} .^{-3}$. It would appear that the density given by Groth is a misprint and should really refer to the dihydrate, for which he does not give any density. Systematic absences were $h 0 l$ when $l$ is odd and $h k 0$ when $(h+k)$ is odd. These are characteristic of two space groups, $C_{2 v}^{9}-P 2_{1} c n$ and $D_{2 h}^{16}$-Pmen. Neither of these space groups is in the class 222 quoted by Groth.

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The atomic scattering factors of $\mathrm{Au}^{+}$and Hg++. By W. G. Henry, Division of Applied Chemistry, National Research Council, Ottawa, Canada
(Received 4 September 1953)

Total atomic scattering factors, $f$, for coherent radiation have been calculated for $\mathrm{Au}^{+}$and $\mathrm{Hg}^{++}$by the numerical integration (Scarborough, 1950) of the integral (James \& Brindley, 1931)

$$
f=\int_{0}^{\infty} P^{2}(r) \frac{\sin \mu r}{\mu r} d r
$$

where $\mu=4 \pi \sin \theta / \lambda$ and $P^{2}(r)$ is the radial charge density.

The radial charge density $P^{2}(r)$ has been determined by the method of the self-consistent field, without exchange, for $\mathrm{Hg}^{++}$by Hartree \& Hartree (1935) and for $\mathrm{Au}^{+}$by Henry (unpublished work). The effect on the
scattering factor of including exchange is small (Brindley \& Ridley, 1938). Results are given in Table 1.

Table 1. Atomic scattering factors
(Integration error $\pm 0.02$ )

| $\frac{\sin \theta}{\lambda} \times 10^{-8}$ | $\mathrm{Au}^{+}$ | $\mathrm{Hg}^{++}$ | $\frac{\sin \theta}{\lambda} \times 10^{-8}$ | $\mathrm{Au}^{+}$ | $\mathrm{Hg}^{++}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 78.00 | 78.00 | 0.7 | 37.46 | 37.98 |
| 0.1 | 74.26 | 74.71 | 0.8 | 33.66 | 34.38 |
| 0.2 | $\mathbf{6 6 . 3 2}$ | 67.21 | 0.9 | 30.52 | 31.20 |
| 0.3 | 58.35 | 59.18 | 1.0 | 27.62 | 28.23 |
| 0.4 | 51.62 | 52.27 | 1.1 | 25.27 | 25.86 |
| 0.5 | 46.07 | 46.65 | 1.2 | 23.28 | 23.36 |
| 0.6 | 41.42 | 41.97 |  |  |  |

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On the crystal and molecular structure of fluorene. By George M. Brown and Marlyn H. Bortiner, Department of Chemistry, University of Maryland, College Park, Maryland, U.S.A.
(Received 6 October 1953)

According to the X-ray analysis of crystalline fluorene by Iball (1936), the two six-membered rings in the fluorene molecule are each tilted up about $20^{\circ}$ out of the plane of the five-membered ring. In contrast, recent stereochemical (Weisburger et al., 1950) and ultra-violet spectroscopic (Merkel \& Wiegand, 1947, 1948) studies on fluorene and an X-ray analysis (Fenimore, 1948) of the closely related bifluorene (dibiphenylene-ethylene) molecule indicate a uniplanar structure for the fluorene carbon skeleton. Since the details of the fluorene structure are of some interest from the point of view of valence theory and chemical reactivity (Lothrop, 1939) and in relation to carcenogenicity of fluorene derivatives (Miller et al., 1949; Sandin et al., 1952), a new X-ray analysis of fluorene has been undertaken in this laboratory.

Crystals of fluorene have been found to be orthorhombic, of space group Pna or Pnam, with four molecules per unit cell, and with $a=8.50, b=5.71, c=19 \cdot 00 \AA$, in essential agreement with the data of Iball. With the use of the Weissenberg multiple-film technique and $\mathrm{Cu} K \alpha$ radiation, data have been obtained for the zero and higher layers for rotations about the three principal axes. In all, 210 reflections have been recorded and their intensities estimated visually, the number being limited so far because of difficulties in preserving the volatile crystal specimens. Limited success in preserving the crystals was attained by coating them with diluted colorless nail polish.

The distribution of peaks in a Patterson projection [010] strongly suggested space group Pnam. The planar model below (similar to Iball's first trial structure and to Fenimore's model for half the bifluorene molecule) was adopted. Satisfactory preliminary agreement between calculated and observed structure factors for the reflec-

tions of the three principal zones was obtained for a structure having the model molecule oriented parallel to $z$ with the point $O$ at $x / a=0.353, y / b=0.431$, $z / c=0.250$, with an angle of $30.5^{\circ}$ between the line $O P$ and the $y$ axis. The reliability factor $\Sigma\left(\left|\left|F_{o}\right|-\left|F_{c}\right|\right|\right) \div \Sigma\left|F_{o}\right|$ was $0 \cdot 22$. The value of $B$ in the temperature factor was $4.6 \times 10^{-16} \mathrm{~cm}^{2}$.

Electron-density projections [100], [010], and [001] were computed using X-RAC. The [100] projection shows each molecule, but not each atom, resolved. In the [010] projection carbons $2,3,7,8,10,11,12$, and 13 are clearly resolved, and their positions show the approximate correctness of the angular orientation of the benzene nuclei as given in the model. In the [001] projection, each molecule is seen edgewise as one link in a zigzag chain. The shape and distribution of contours in this projection are consistent only with a structure in which deviations from uniplanarity are no more than trivial.

The essential correctness of the proposed planar structure of fluorene is regarded as established. The process of refinement is being carried out, and efforts are being made to record more of the 1090 reflections theoretically accessible using Cu $K \alpha$ radiation, in the hope of achieving a very accurate structure determination.

We gratefully acknowledge the kindess of Prof. Ray Pepinsky of the Pennsylvania State College in allowing our Patterson and Fourier syntheses to be performed on X-RAC.

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